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CORNING GLASS WORKS

ELECTRO-OPTICS LABORATORY

RALEIGH, NORTH CAROLINA

IMPROVED SCREEN FOR REAR PROJECTION VIEWERS

Technical Report No. - 7

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## Technical Report #7

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Corning Glass Works manufactures several different materials which are being investigated for uses in rear projection screens. Some of these materials are new such as the hollow optical fibers while other approaches are based on more conventional glass products. Theoretical studies are being made to be able to specify, to the material groups in manufacturing, specific characteristics needed to give these materials the desired light scattering properties.

#### I. Theoretical Studies (Mie Scattering)

Some of the materials which are being considered for use in rear projection screens, namely the glass ceramics, Fotoform and Fotoceram, and the sintered glasses, have been determined to have particle sizes in the Mie scattering range. This means particles from 1000 Å to over 20 microns in diameter. The light scattering characteristics of these materials is given by the Mie theory of light scattering<sup>(1)</sup>.

Although this theory is very general it finds primary application when the size of the particle is about equal to or larger than the wavelength of the incident radiation.

The important equations derived by Mie for both the parallel and normal components of polarized light incident on a spherical particle are

$$I_{II}(\theta) = \left| \sum_{n=1}^{\infty} \left\{ A_n \frac{dP_n(x)}{dx} + B_n \left[ x \frac{dP_n(x)}{dx} - (1-x^2) \frac{d^2P_n(x)}{dx^2} \right] \right\} \right|^2 \quad (1)$$

$$I_{\perp}(\theta) = \left| \sum_{n=1}^{\infty} \left\{ A_n \left[ x \frac{dP_n(x)}{dx} - (1-x^2) \frac{d^2P_n(x)}{dx^2} \right] + B_n \frac{dP_n(x)}{dx} \right\} \right|^2 \quad (2)$$

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where  $P_n(x)$  = Legendre polynomials of order  $n$ , with  
 $x = \cos \theta$ , and

$$A_n = \left[ \frac{(-1)^{n+1/2} (2n+1)}{n(n+1)} \right] \begin{bmatrix} S_n(\alpha) \frac{dS_n(\beta)}{d\beta} - m^* S_n(\beta) \frac{dS_n(\alpha)}{d\alpha} \\ \phi_n(\alpha) \frac{dS_n(\beta)}{d\beta} - m^* S_n(\beta) \frac{d\phi_n(\alpha)}{d\alpha} \end{bmatrix} \quad (3)$$

$$B_n = \left[ \frac{(-1)^{n+3/2} (2n+1)}{n(n+1)} \right] \begin{bmatrix} m^* S_n(\alpha) \frac{dS_n(\beta)}{d\beta} - S_n(\beta) \frac{dS_n(\alpha)}{d\alpha} \\ m^* \phi_n(\alpha) \frac{dS_n(\beta)}{d\beta} - S_n(\beta) \frac{d\phi_n(\alpha)}{d\alpha} \end{bmatrix}, \quad (4)$$

where  $S_n(\alpha)$  = Riccati Bessel function =  $\left(\frac{\pi\alpha}{2}\right)^{\frac{1}{2}} J_{n+1/2}(\alpha)$ ,  
 $\phi_n(\alpha)$  = Riccati Hankel function =  $S_n(\alpha) + j(-1)^n \left(\frac{\pi\alpha}{2}\right)^{\frac{1}{2}} J_{-n-1/2}(\alpha)$ ,

and  $J_{n+1/2}(\alpha)$  and  $J_{-n-1/2}(\alpha)$  = Bessel functions of half integral order.

Thus, the only physical parameters are:

$\theta$  = angle between direction of propagation of scattered and the reverse direction of the incident light, as shown in Figure 1,

$$\alpha = \frac{\pi D}{\lambda}, \quad (5)$$

and

$$= m^* \alpha = \alpha (m - jk), \quad (6)$$

where  $D$  = diameter of spherical particle

$\lambda$  = wavelength of incident radiation in surrounding media

$m$  = index of refraction of particle relative to surrounding media

$k$  = extinction coefficient of the particle material

$j = \sqrt{-1}$ .

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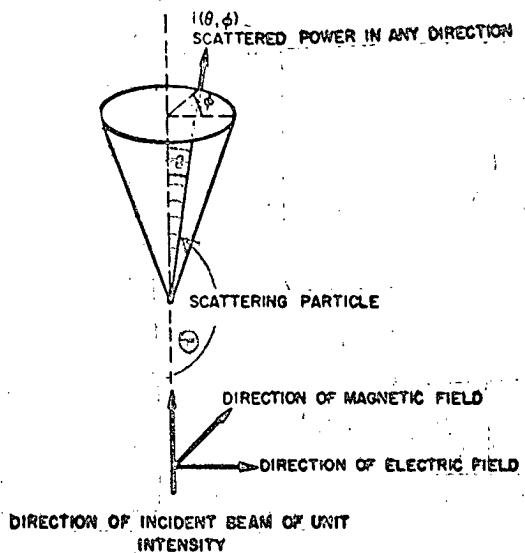
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Figure 1

To solve any given problem requires tables of the real and imaginary parts of  $A_n$  and  $B_n$  and tables of the Legendre polynomials and their first derivatives<sup>(2-6)</sup>. These are then combined using a desk calculator or preferably a large digital computer into values of  $I_{II}(\theta)$  and  $I_L(\theta)$  from which the angular distribution function  $I(\theta)$  is obtained

$$I(\theta) = \frac{I_{II}(\theta) + I_L(\theta)}{2\pi\alpha K} \quad (7)$$

where the scattering coefficient, i. e., the ratio of the scattering cross section to the geometrical cross section is,

$$K = \frac{2}{\alpha^2} \sum_{n=1}^{\infty} \frac{n^2(n+1)^2}{2n+1} (|A_n|^2 + |B_n|^2), \quad (8)$$

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Hartel<sup>(7)</sup> suggested that Equations (1) and (2) could be simplified in form by the repeated use of recurrence relationships between the derivatives and products of Legendre polynomials. Recently Chu and Churchill succeeded in rearranging the Mie equations for the angular distribution of radiation scattered by nonabsorbing spheres in terms of a series of Legendre polynomials<sup>(8)</sup>,

$$f(\theta) = \frac{1}{4\pi} \sum_{n=0}^{\infty} a_n(\alpha, \beta) P_n(\cos\theta) = \frac{1}{4\pi} + \frac{1}{4\pi} \sum_{n=1}^{\infty} a_n P_n(\cos\theta), \quad (9)$$

where the coefficients,  $a_n$ , are functions of  $\alpha$  and but not of the angle and are given by

$$a_n = \frac{(2)(-1)^n}{\alpha^2 K(\alpha, \beta)} \sum_{j=1}^{\infty} \sum_{k=1}^{\infty} \left( \frac{2}{1 + \delta_{jk}} \right) \left\{ (2n+1) \left[ \frac{j(j+1) + k(k+1) - n(n+1)}{2} \right]^2 w_{jkn} w_{jk} + v_{jkn} v_{jk} \right\}, \quad (10)$$

where

$$\delta_{jk} = \begin{cases} 0 & \text{for } j \neq k \\ 1 & \text{for } j = k \end{cases}, \quad (11)$$

$$w_{jk} = \operatorname{Re}(A_j)\operatorname{Re}(A_k) + \operatorname{Im}(A_j)\operatorname{Im}(A_k) + \operatorname{Re}(B_j)\operatorname{Re}(B_k) + \operatorname{Im}(B_j)\operatorname{Im}(B_k), \quad (12)$$

$$v_{jk} = \operatorname{Re}(A_j)\operatorname{Re}(B_k) + \operatorname{Im}(A_j)\operatorname{Im}(B_k) + \operatorname{Re}(B_j)\operatorname{Re}(A_k) + \operatorname{Im}(B_j)\operatorname{Im}(A_k) \quad (13)$$

$$w_{jkn} = 0, \quad \text{if } j + k - n \neq 2r, \quad r = 0, 1, 2, \dots, k, \quad (14)$$

$$w_{jkn} = \frac{(-1)^{j+n-k} (-1)^{k+n-j} (-1)^{j+k-n} \left( \frac{j+k+n}{2} \right)^2}{(-1)^{j+k+n+1} \left[ \left( \frac{j+n-k}{2} \right) \left( \frac{k+n-j}{2} \right) \left( \frac{j+k-n}{2} \right) \right]^2} \quad \text{if } j + k - n = 2r, \quad r = 0, 1, 2, \dots, k. \quad (15)$$

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$$v_{jkn} = 0, \quad \text{if } j+k-n \neq 2r+1, \quad r=0,1,2\cdots k,$$

(16)

and

(17)

$$v_{jkn} = \frac{(2n+1)(j+k-n)(j+n-k+1)(k+n-j+1) \angle j+n-k+1) \angle k+n-j+1) \angle j+k-n-1) \left( \angle \frac{j+k+n+1}{2} \right)^2}{4(j+k+n+1) \left[ \left( \angle \frac{j+n-k+1}{2} \right) \left( \angle \frac{k+n-j+1}{2} \right) \left( \angle \frac{j+k-n-1}{2} \right) \right]^2}$$

if  $j+k-n=2r+1, \quad r=0,1,2\cdots k.$

where       $\text{Im}$  = Imaginary Part,

Re = Real part,

 $\angle$  = factorial.

The advantage of expressing the angular distribution of intensity in the form of Equation (9) rather than Equations (1) and (2) is obvious. The intensity at any angle for which the Legendre polynomials are available can be computed from a set of coefficients for a given  $\alpha$  and  $m$ .

In general, the number of significant terms in the series is about equal to  $2\alpha$ . The Legendre polynomials are available at one-degree intervals, and their behavior is better known and interpolation with respect to angle can be done more accurately than with  $I_{11}$  and  $I_1$ ;  $I(\theta)$  or the tabulated derivatives of the polynomials. Interpolation with respect to  $\alpha$  and  $\beta$  is also easier with the coefficients,  $a_n$  than with  $I_{11}$  and  $I_1$  or  $I(\theta)$  and need be carried out but once for all angles.

Additional advantages of the representation of the angular distribution of scattered radiation by Equation (9) can be noted. The power scattered into any region, and in particular into the forward and backward hemisphere, can be obtained by simple analytical integration. By assuming

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that a particle receives power only from adjacent particles having the same multiple-scattering distribution, Hartel developed the following equation in terms of the same coefficients,  $a_n$ , for the angular distribution of the k-th scattered radiation in a dense dispersion:

$$f_k(\theta) = \frac{1}{4\pi} \left[ 1 + \sum_{n=1}^{\infty} \frac{a_n^k}{(2n+1)^{k-1}} P_n(\cos\theta) \right] \quad (18)$$

As complex as Equations (9-17) look, it is much simpler to evaluate (9) than Equations (1) and (2) because only values of  $A_n$  and  $P_n(\cos\theta)$  are required and are available<sup>(9-11)</sup>. However the tables of  $A_n$  and  $P_n(\cos\theta)$  are very limited while the tables of  $A_n$  and  $B_n$  are by far more complete, i.e., they are finer divisions of  $\alpha$  and  $m$  and they cover a larger range of particle sizes. Therefore, we will use the Mie equations for single scattering investigation and to obtain data for which tables of angular coefficients do not exist; we will utilize the angular coefficients primarily for a study of multiple scattering.

Thus far a computer program to compute  $I_{||}(\theta)$ ,  $I_{\perp}(\theta)$ ,  $(I_{||}(\theta) + I_{\perp}(\theta))/2$  and the percent polarization, has been written and tested. This has been used to compute the scattering function for  $m = 1.20$ ,  $\alpha = 1, 2, 3, 5, 8$ , and  $10$ . Some of the output data is given in the data appendix. The negative sign in the percent polarization column indicates the light is polarized normal to the plane the angle  $\theta$  is measured in. The computer program also computes the screen efficiency, EFF., which is the ratio of the intensity scattered into the forward hemisphere to the incident intensity  $I_0$ .

$$\text{EFF}(m, \alpha) = \frac{\int_{\pi/2}^{\infty} I(m, \alpha, \theta) d\theta}{\int_0^{\pi} I(m, \alpha, \theta) d\theta} = \frac{1}{I_0} \int_{\pi/2}^{\pi} I(\theta) d\theta \quad (19)$$

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It is convenient to normalize the scattering function to reflect the ratio of the intensity of light scattered by a given particle, as a function of angle, to a perfect diffusor which radiates uniformly in all directions.

This ratio is called Gain and is defined as

$$\text{Gain } (m, \alpha, \theta) = \frac{I_0}{\frac{1}{\pi} \int_0^\pi I(m, \alpha, \theta) d\theta} \quad (20)$$

These computations were also made and the gain characteristics of the light scattering functions are given as the second page of the computer print out. The angular gain characteristics for several different particle sizes are given in Figure 2.

Another parameter of interest is the relation between gain, at  $\theta = 0$ , and  $\alpha$ , Figure 3. This is a simpler measure of the scattering function and easier to consider in relation to other parameters. The efficiency of different materials made up of particles of various sizes are given in Figure 4. It is surprising that these materials appear to be so efficient at such low values of  $\alpha$  and gain, Figure 5. This indicates that if the light scattering properties of screens made from these particles are not significantly different from the single particle characteristics it may be possible to manufacture highly efficient screens which have broad viewing angles and are relatively insensitive to ambient light. Obviously a complete analysis and discussion of volume Mie scattering must be left to later when more data is available.

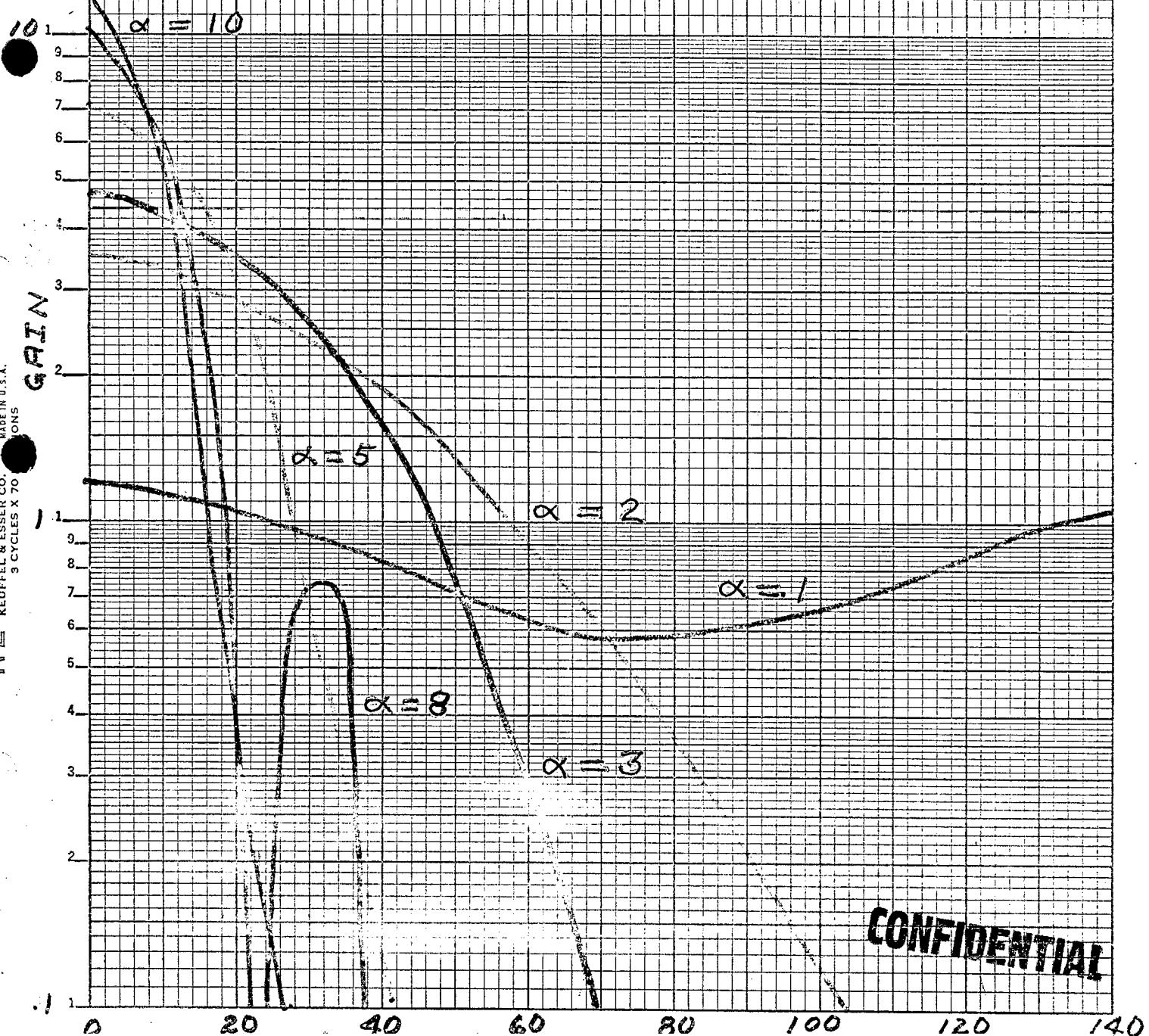
This type of analysis will be carried out next period. We also expect to be able to start a study of multiple scattering and determine the major characteristics of it, in terms of materials and viewing parameters.

GAIN

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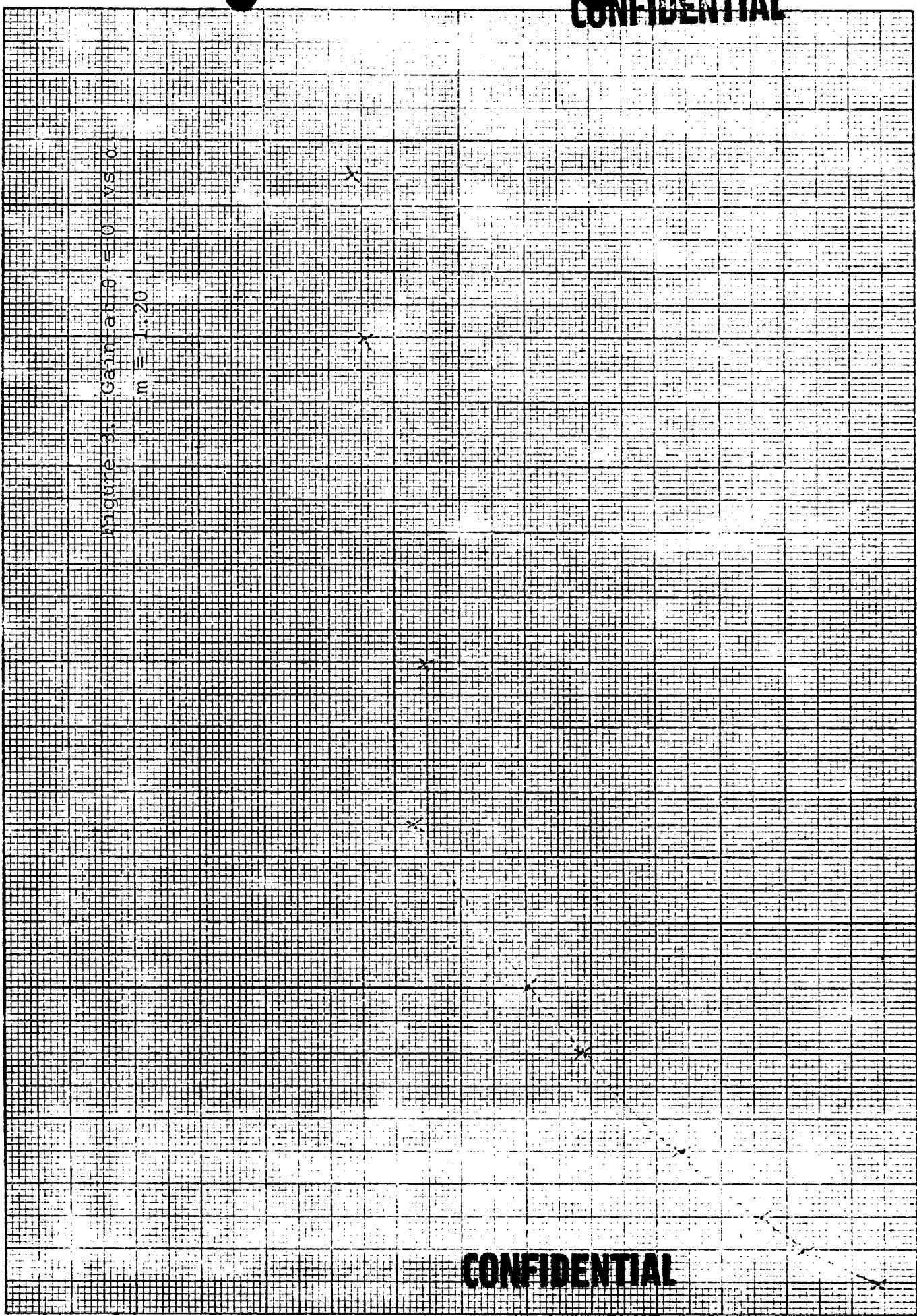
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Figure 2. Angular gain characteristics for several different particle sizes.  $m = 1.20$



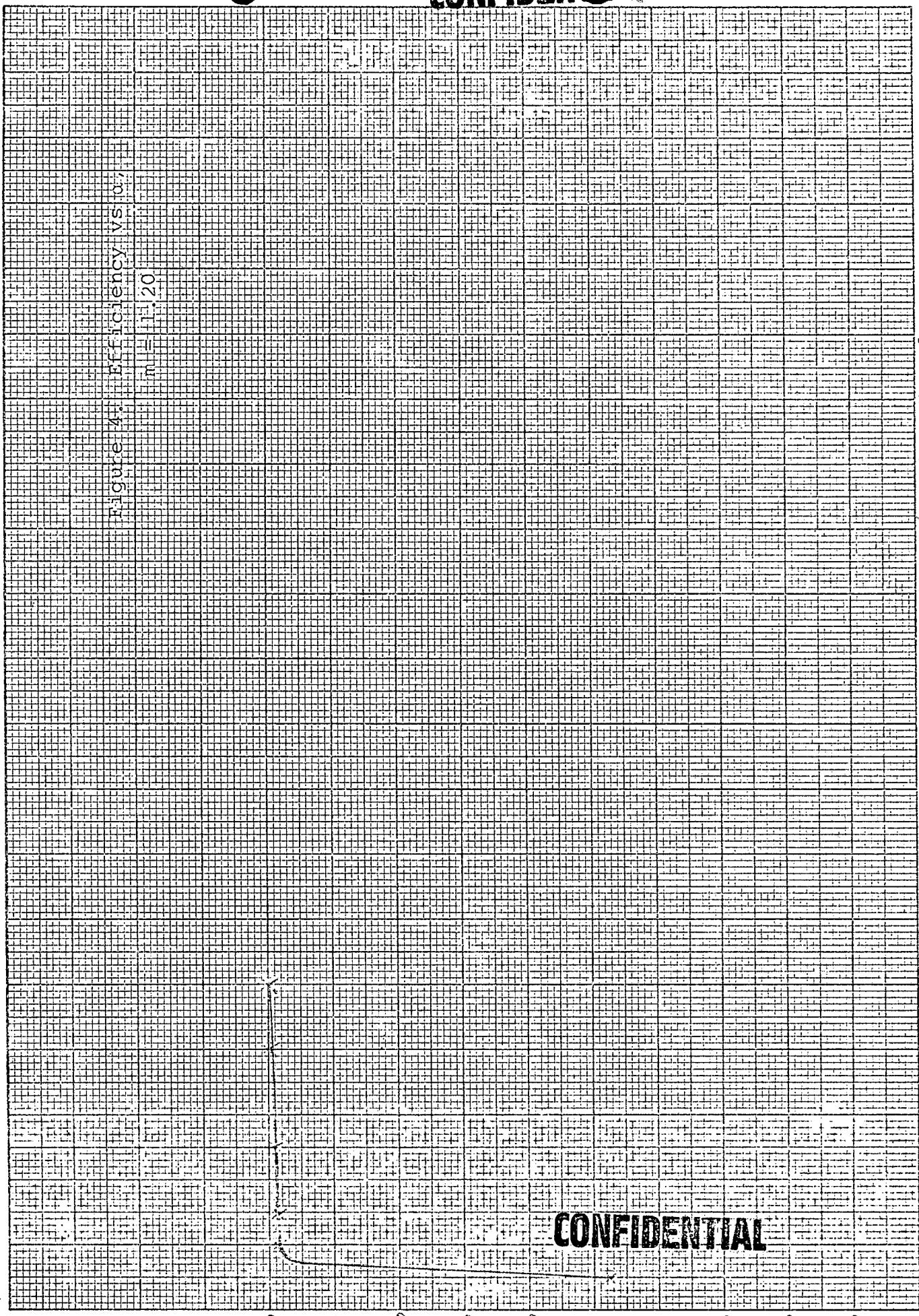
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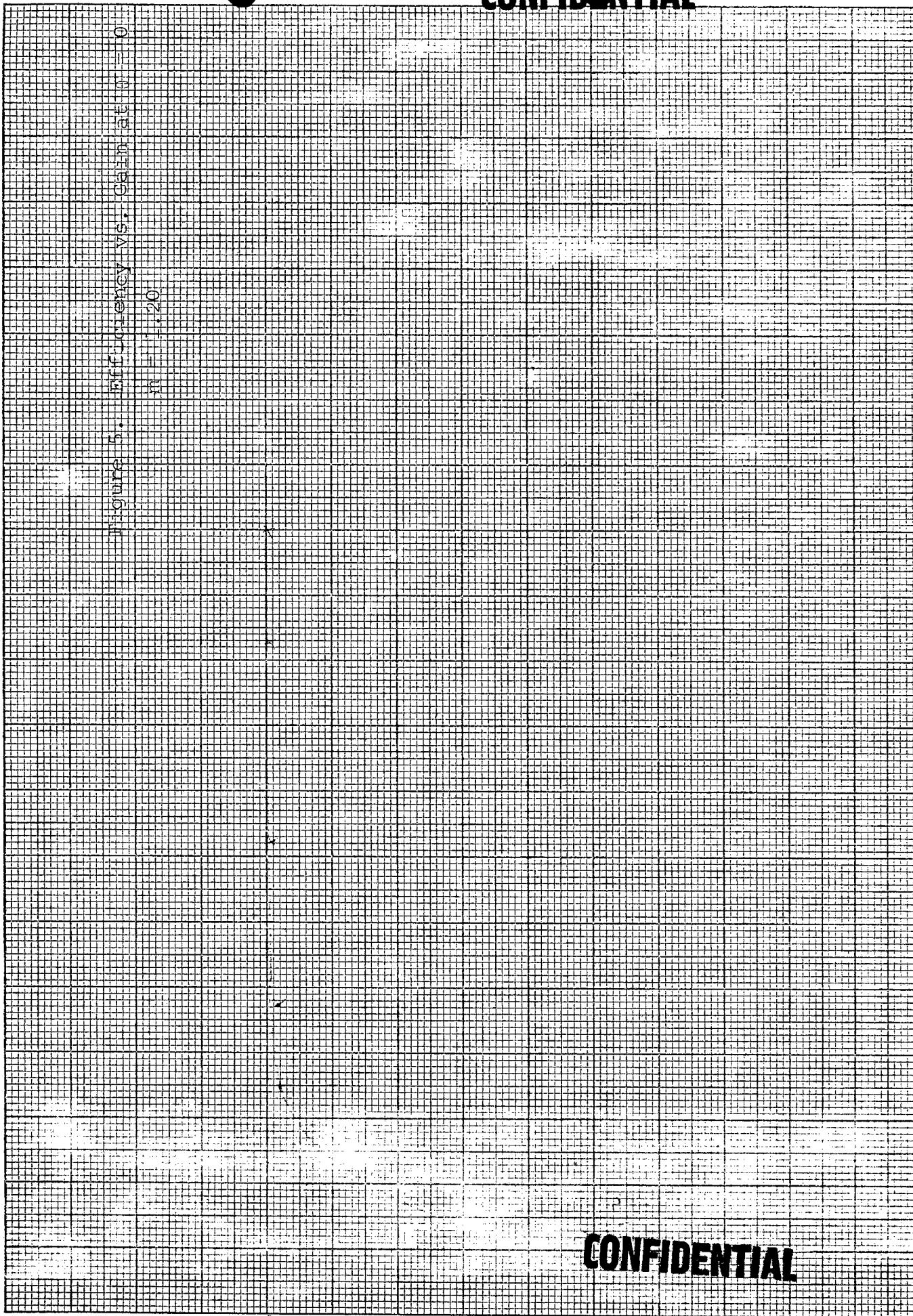


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In the final report covering the second phase of our program devoted to theoretical studies, Mie scattering will be outlined in greater detail. We will also include a complete discussion of the results obtained using the computer programs. Throughout this study emphasis will be on applying these results and generating requirements for samples of various materials from our manufacturing facilities.

## II. CGW Materials

### A. Hollow Fibers

We have begun to experimentally investigate the plating of hollow fibers. This work is being done in conjunction with the Microcircuits Group, in the Raleigh facility, who have much of the necessary technology.

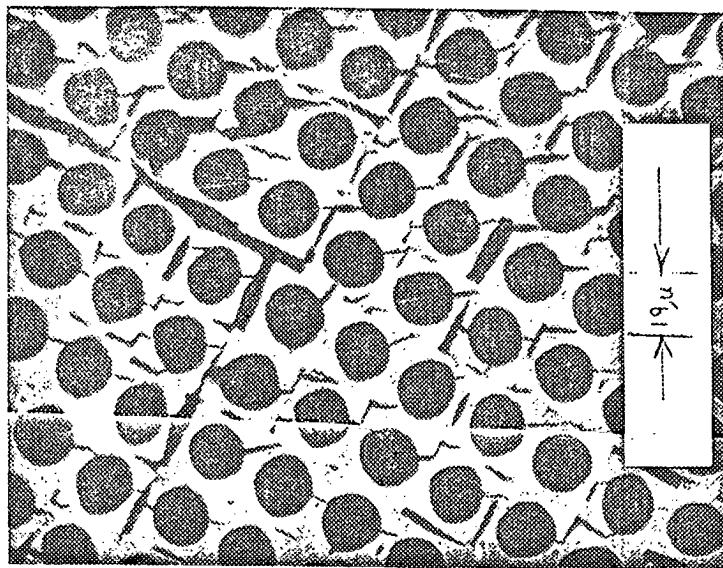
Samples of individual fibers, Figure 6a, 6b, as well as a small array, Figure 6c, have been supplied to this group for preliminary investigations. More fibers and fiber arrays will be requested next period to continue this work. Results of the feasibility of placing highly reflective coatings in small diameter tubes are expected by the end of the quarter.

In addition to the vapor plating techniques already described<sup>(12)</sup> others will be tried. One involves the floating of millimicron sized metallic particles into the tubes using ether or a similiar inert reagent. By heating the tubes in a RF field the carrier liquid will evaporate and the metal vapor will "condense" on the walls.

### B. Porous Vycor

Photomicrographs of the samples delivered sometime ago were made at our facility in Corning, New York.

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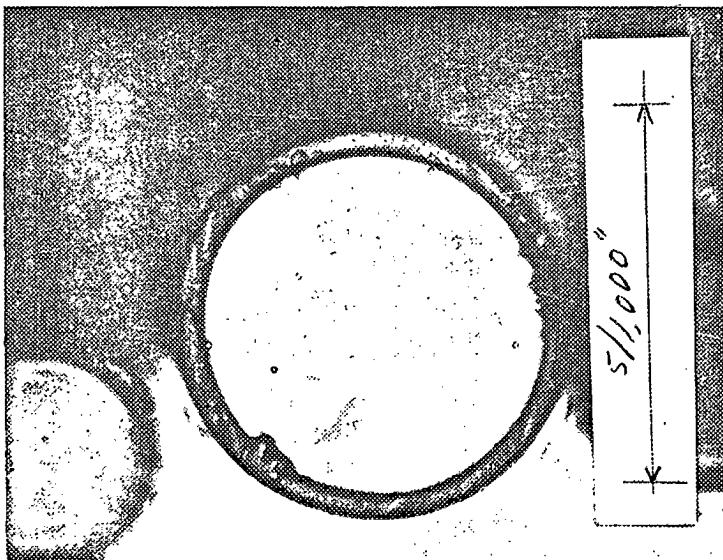
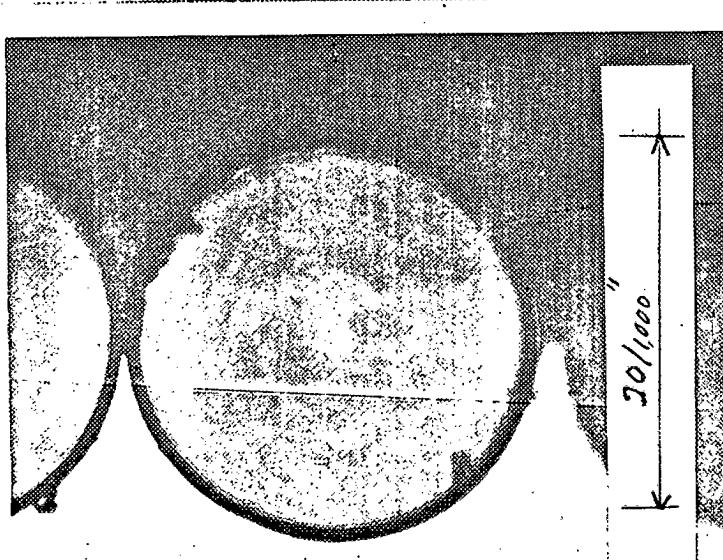


Figure 6. Photomicrographs of two samples of hollow fibers and one fiber array to be used in preliminary plating studies.



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Figure 7 shows a top view, at a magnification of 625x. The larger pores produced by leaching the glass are clearly visible, as they are in cross sectional views in Figures 7b at 310x and 7c at 625x. Most of the particles responsible for the scattering are so small, about 50 to 100 Angstroms in diameter that they are not visible. We are waiting further photomicrographs taken through the electron microscope which may show particles near this size range.

Full interpretation of these must wait for the other pictures as well as a detailed study of the ones just recently obtained.

#### C. Other Materials

Next period we will obtain samples of the following materials

1. Sintered Glass
2. Fotoform and Fotoceram
3. Glass Ceramics

These will be investigated and used in conjunction with the theoretical work to formulate specifications for specific materials to the manufacturing groups in Corning, New York.

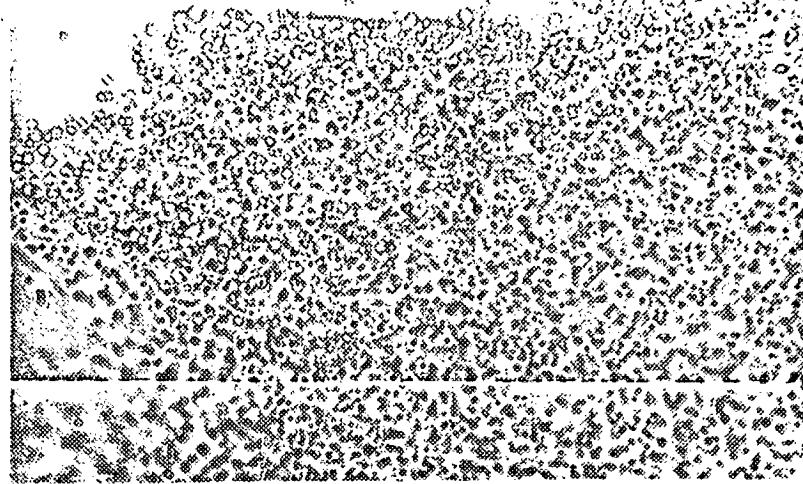
### III. Instrumentation

#### A. Goniophotometer

Construction of this instrument is on schedule and due to be completed by March 1. All of the electronics for data processing and display are being assembled, along with power supplies and controls, into a control console. Subsequent testing, alignment, and calibration are scheduled to be complete by April 1.

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**Figure 7. Photomicrographs of porous Vycor brand glass, a, 625x; b, 310x; c, 625x.**

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B. Modulation Transfer Function Analyzer

Design has started on the instrument to make the sine-wave target.<sup>(12)</sup> Several different types of light modulating techniques have been investigated for this application. One optical system is shown schematically in Figure 8.

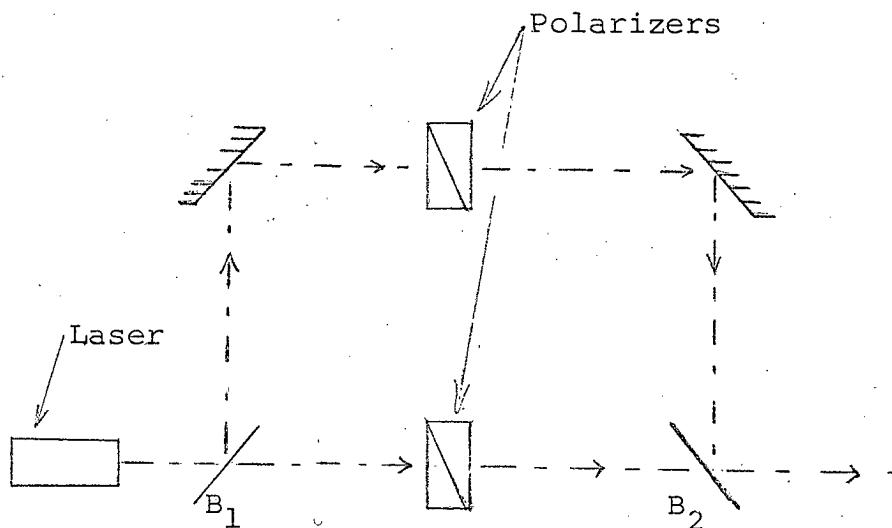


Figure 8

Light from the laser, which is polarized, is divided into two beams by the first beam splitter. Each passes through a polarizing filter which attenuates that particular beam depending on the orientation of its axis with the direction of polarization of the laser beam, i. e.,

$$I(\theta) = K I_0 \cos \theta$$

where  $I(\theta)$  is the intensity through the filter depending on the angle,  $\theta$ , between the direction of polarization of the light and the axis of the filter;  $K$  is a correction for the neutral density of the filter regardless of polarization.

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Thus to sinusoidally modulate a beam only requires the polarizing filter be rotated at a constant angular speed  $\omega$ . The frequency of the modulated light  $\omega_m$  will be just  $2\omega$ .

The other beam is used to add a constant light level to this modulated signal thereby setting the operating point on the linear portion of the characteristic curve of the film.

The remaining optics is used to illuminate a slit and transfer this image onto the film. The sine-wave transmission pattern on the strip of film is accomplished by moving it at constant speed across the variable intensity slit image. The construction of this device will start next period.

The components for the MTF analyzer and initial machine shop work will also begin then.

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DATA APPENDIX

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SCATTERING FUNCTION FOR A = 1, M = 1.20

ANGLE DEGREES	INTENSITY 1 PARALLEL	INTENSITY 1 NORMAL	INTENSITY 2 UNPOLARIZED	INTENSITY 3 Polarization
1	•1322709E-01	•1322709E-01	•1322709E-01	•000
2	•132658E-01	•132080E-01	•132369E-01	•218
3	•132508E-01	•130202E-01	•131355E-01	•877
4	•132261E-01	•127094E-01	•129677E-01	•992
5	•131923E-01	•122792E-01	•127357E-01	•584
6	•131501E-01	•117347E-01	•124424E-01	•687
7	•131004E-01	•110831E-01	•120917E-01	•341
8	•130442E-01	•103332E-01	•116887E-01	•596
9	•129827E-01	•949648E-02	•112396E-01	•508
10	•129173E-01	•858648E-02	•107518E-01	•139
11	•128490E-01	•761961E-02	•102343E-01	•548
12	•127794E-01	•661491E-02	•969717E-02	•785
13	•127096E-01	•559412E-02	•915189E-02	•874
14	•126410E-01	•458145E-02	•861124E-02	•796
15	•125746E-01	•360328E-02	•808829E-02	•454
16	•125117E-01	•268756E-02	•759964E-02	•635
17	•124530E-01	•186311E-02	•715808E-02	•971
18	•123994E-01	•115857E-02	•677902E-02	•909
19	•123515E-01	•601292E-03	•647643E-02	•715
20	•123098E-01	•215933E-03	•626287E-02	•552
21	•122744E-01	•231088E-04	•614878E-02	•624
22	•122455E-01	•379088E-04	•614173E-02	•382
23	•122230E-01	•268556E-03	•624578E-02	•700
24	•122065E-01	•715245E-03	•646090E-02	•929
25	•121957E-01	•136927E-02	•678251E-02	•811
26	•121900E-01	•221261E-02	•720133E-02	•274
27	•121887E-01	•321794E-02	•770335E-02	•226
28	•121911E-01	•434923E-02	•827018E-02	•410
29	•121963E-01	•556296E-02	•887964E-02	•351
30	•122035E-01	•680980E-02	•950665E-02	•368
31	•122118E-01	•803687E-02	•101243E-01	•618
32	•122204E-01	•919027E-02	•107053E-01	•152
33	•122286E-01	•102179E-01	•112232E-01	•957
34	•122357E-01	•110724E-01	•116540E-01	•990
35	•122411E-01	•117136E-01	•119774E-01	•202
36	•122446E-01	•121111E-01	•121778E-01	•548
37	•122458E-01	•122458E-01	•122458E-01	•000

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## SCATTERING FUNCTION FOR A = 1, M = 1.20

ANGLE DEGREES	GAIN PARALLEL	GAIN NORMAL	GAIN UNPOLARIZED	PERCENT POLARIZATION
1	1.05	2.01	1.38	0.00
2	1.05	2.00	1.38	.218
3	1.05	1.98	1.37	.877
4	1.05	1.93	1.35	1.992
5	1.05	1.86	1.33	3.584
6	1.04	1.78	1.30	5.687
7	1.04	1.68	1.26	8.341
8	1.03	1.57	1.22	11.596
9	1.03	1.44	1.17	15.508
10	1.02	1.30	1.12	20.139
11	1.02	1.15	1.07	25.548
12	1.01	1.00	1.01	31.785
13	1.01	.85	.95	38.874
14	1.00	.69	.90	46.796
15	1.00	.54	.84	55.454
16	.75	.40	.79	64.635
17	.80	.28	.74	73.971
18	.85	.17	.70	82.909
19	.90	.09	.67	90.715
20	.95	.03	.65	96.552
21	1.00	.97	.00	99.624
22	1.05	.97	.00	99.382
23	1.10	.97	.04	95.700
24	1.15	.97	.10	88.929
25	1.20	.97	.20	79.811
26	1.25	.97	.33	69.274
27	1.30	.97	.48	58.226
28	1.35	.97	.66	47.410
29	1.40	.97	.84	37.351
30	1.45	.97	1.03	28.368
31	1.50	.97	1.22	20.618
32	1.55	.97	1.39	14.152
33	1.60	.97	1.55	8.957
34	1.65	.97	1.63	4.990
35	1.70	.97	1.78	2.202
36	1.75	.97	1.84	0.548
37	1.80	.97	1.86	0.000

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## SCATTERING FUNCTION FOR A = 2, M = 1, 20

ANGLE DEGREES	INTENSITY		
	1 PARALLEL	2 NORMAL	3 UNPOLARIZED
	PERCENT POLARIZATION		
1	• 341572E-02	• 341572E-02	• 341572E-02
2	• 336308E-02	• 334681E-02	• 336494E-02
3	• 329817E-02	• 314955E-02	• 322386E-02
4	• 320079E-02	• 285099E-02	• 302589E-02
5	• 315946E-02	• 249145E-02	• 282546E-02
6	• 327471E-02	• 211789E-02	• 269630E-02
7	• 368353E-02	• 177544E-02	• 272949E-02
8	• 456470E-02	• 149828E-02	• 303149E-02
9	• 614487E-02	• 130123E-02	• 372305E-02
10	• 870494E-02	• 117421E-02	• 493957E-02
11	• 125861E-01	• 108204E-02	• 683408E-02
12	• 181950E-01	• 972366E-03	• 958369E-02
13	• 260067E-01	• 794572E-03	• 134006E-01
14	• 365651E-01	• 531987E-03	• 185485E-01
15	• 504785E-01	• 248478E-03	• 253634E-01
16	• 684094E-01	• 148497E-03	• 342789E-01
17	• 910581E-01	• 646716E-03	• 458524E-01
18	• 119137E-00	• 243982E-02	• 607884E-01
19	• 153336E-00	• 656921E-02	• 799527E-01
20	• 194280E-00	• 144596E-01	• 104370E-00
21	• 242477E-00	• 279172E-01	• 155197E-00
22	• 298256E-00	• 490701E-01	• 173663E-00
23	• 361713E-00	• 802385E-01	• 220976E-00
24	• 432643E-00	• 123729E-00	• 278186E-00
25	• 510489E-00	• 181561E-00	• 346025E-00
26	• 594305E-00	• 255140E-00	• 424722E-00
27	• 682727E-00	• 344919E-00	• 513823E-00
28	• 773987E-00	• 450092E-00	• 612040E-00
29	• 865939E-00	• 568371E-00	• 717155E-00
30	• 956130E-00	• 695904E-00	• 826017E-00
31	• 104189E-01	• 827367E-00	• 934632E-00
32	• 112049E-01	• 956261E-00	• 103837E-01
33	• 118921E-01	• 107538E-01	• 113230E-01
34	• 124559E-01	• 117747E-01	• 121153E-01
35	• 128751E-01	• 125586E-01	• 127168E-01
36	• 131334E-01	• 130521E-01	• 130928E-01
37	• 132207E-01	• 132207E-01	• 132207E-01

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ANGLE DEGREES	GAIN PARALLEL	GAIN NORMAL	GAIN UNPOLARIZED	PERCENT POLARIZATION
1	0.00	0.01	0.01	0.000
2	5.0	0.00	0.01	5.38
3	10.0	0.00	0.01	2.304
4	15.0	0.00	0.01	5.780
5	20.0	0.00	0.00	11.821
6	25.0	0.00	0.00	21.452
7	30.0	0.00	0.00	34.953
8	35.0	0.01	0.00	50.575
9	40.0	0.01	0.00	65.049
10	45.0	0.02	0.00	76.228
11	50.0	0.03	0.00	84.166
12	55.0	0.04	0.00	89.853
13	60.0	0.06	0.00	94.070
14	65.0	0.09	0.00	97.131
15	70.0	0.12	0.00	99.020
16	75.0	0.17	0.00	99.566
17	80.0	0.22	0.00	98.589
18	85.0	0.29	0.00	95.986
19	90.0	0.38	0.02	91.783
20	95.0	0.48	0.05	86.145
21	100.0	0.60	0.09	79.350
22	105.0	0.74	0.17	71.744
23	110.0	0.90	0.28	63.689
24	115.0	1.08	0.44	55.522
25	120.0	1.27	0.64	47.529
26	125.0	1.48	0.91	39.927
27	130.0	1.70	1.23	32.871
28	135.0	1.93	1.60	26.460
29	140.0	2.16	2.02	20.746
30	145.0	2.39	2.48	15.751
31	150.0	2.60	2.95	11.476
32	155.0	2.80	3.41	7.907
33	160.0	2.97	3.83	5.026
34	165.0	3.11	4.20	2.811
35	170.0	3.22	4.43	1.244
36	175.0	3.28	4.65	0.310
37	180.0	3.30	4.71	0.000

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## SCATTERING FUNCTION FOR A = 3, M = 1.20

ANGLE DEGREES	INTENSITY 1 PARALLEL	INTENSITY 2 NORMAL	INTENSITY 3 UNPOLARIZED	PERCENT POLARIZATION
1 2	•101300E 00	•101300E 00	•101300E 00	•000
5°	•101794E 00	•100485E 00	•101139E 00	•647
10°	•103364E 00	•980814E-01	•100722E 00	•622
15°	•106250E 00	•941991E-01	•100224E 00	•6.012
20°	•110791E 00	•890028E-01	•998971E-01	•10.905
25°	•117331E 00	•8266869E-01	•100009E 00	•17.320
30°	•126099E 00	•754605E-01	•100780E 00	•25.123
35°	•137075E 00	•675487E-01	•102312E 00	•33.977
40°	•149846E 00	•592160E-01	•104531E 00	•43.350
45°	•163488E 00	•508082E-01	•107148E 00	•52.581
50°	•176493E 00	•427980E-01	•109645E 00	•60.967
55°	•186786E 00	•358062E-01	•111296E 00	•67.827
60°	•191863E 00	•305709E-01	•111217E 00	•72.512
65°	•189116E 00	•278383E-01	•108477E 00	•74.337
70°	•176361E 00	•281794E-01	•102270E 00	•72.446
75°	•152610E 00	•317824E-01	•921963E-01	•65.527
80°	•119073E 00	•383321E-01	•787029E-01	•51.295
85°	•803405E-01	•471549E-01	•637477E-01	•26.028
90°	•456116E-01	•578467E-01	•517292E-01	-11.826
95°	•298057E-01	•715813E-01	•506935E-01	-41.204
100°	•542733E-01	•931781E-01	•737257E-01	-26.384
105°	•146814E 00	•133781E 00	•140298E 00	4.644
110°	•340693E 00	•213668E 00	•277181E 00	22.913
115°	•672400E 00	•364350E 00	•518375E 00	29.713
120°	•117806E 01	•628849E 00	•903456E 00	30.395
125°	•188863E 01	•105904E 01	•147383E 01	28.143
130°	•282424E 01	•170927E 01	•226676E 01	24.593
135°	•398846E 01	•262625E 01	•330735E 01	20.593
140°	•536335E 01	•383637E 01	•459986E 01	16.598
145°	•690638E 01	•533282E 01	•611960E 01	12.856
150°	•855019E 01	•706556E 01	•780788E 01	9.507
155°	•102058E 02	•893774E 01	•957178E 01	6.624
160°	•117693E 02	•108108E 02	•112900E 02	4.245
165°	•131320E 02	•125192E 02	•128256E 02	2.368
170°	•141913E 02	•136932E 02	•140423E 02	1.061
175°	•148637E 02	•147851E 02	•148244E 02	•265
180°	•150943E 02	•150943E 02	•150943E 02	•000

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## SCATTERING FUNCTION FOR A = 3, M = 1.020

ANGLE DEGREES	GAIN PARALLEL	GAIN NORMAL	GAIN UNPOLARIZED	PERCENT POLARIZATION
1	• 9768	EFF. 1 = • 9768	EFF. 2 = • 9883	EFF. 3 = • 9821
2	• 03	• 03	• 03	• 000
3	• 03	• 03	• 03	• 647
4	• 03	• 03	• 03	2.622
5	• 03	• 03	• 03	6.012
6	• 03	• 03	• 03	10.905
7	• 04	• 02	• 03	17.320
8	• 04	• 02	• 03	25.123
9	• 05	• 02	• 03	33.977
10	• 05	• 01	• 03	43.350
11	• 05	• 01	• 03	52.581
12	• 06	• 01	• 04	60.967
13	• 06	• 01	• 04	67.827
14	• 06	• 01	• 04	72.512
15	• 05	• 01	• 03	74.337
16	• 05	• 01	• 03	72.446
17	• 04	• 01	• 02	65.527
18	• 02	• 01	• 02	51.295
19	• 01	• 02	• 01	26.028
20	• 01	• 02	• 01	-11.826
21	• 01	• 03	• 02	-41.204
22	• 04	• 05	• 05	-26.384
23	• 11	• 08	• 10	4.644
24	• 22	• 14	• 18	22.913
25	• 39	• 24	• 32	29.713
26	• 64	• 41	• 53	30.395
27	• 95	• 66	• 82	28.143
28	1.35	1.01	1.19	24.593
29	1.40	1.81	1.48	20.593
30	1.45	2.34	2.07	16.598
31	1.50	2.90	2.74	12.856
32	1.55	3.46	3.46	9.507
33	1.60	3.99	4.19	6.624
34	1.65	4.45	4.64	4.245
35	1.70	4.81	5.39	2.388
36	1.75	5.04	5.73	1.061
37	1.80	5.11	5.85	0.265
				5.46
				0.00

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